Efficient Snapshot Differential Algorithms for Data Warehousing

Wilbur Juan Labio
Computer Science Dept.
Stanford, CA 94305
wilburt@cs.stanford.edu

Hector Garcia-Molina
Computer Science Dept.
Stanford, CA 94305
hector@cs.stanford.edu

Abstract

Detecting and extracting modifications from information sources is an integral part of data warehousing. For unsophisticated sources, it is often necessary to infer modifications by periodically comparing snapshots of data from the source. Although this snapshot differential problem is closely related to traditional joins, there are significant differences, which lead to simple new algorithms. In particular, we present algorithms that perform compression of records. We also present a window algorithm that works very well if the snapshots are not “very different.” The algorithms are studied via analysis and an implementation of two of them; the results illustrate the potential gains achievable with the new algorithms.

1 Introduction

Warehousing is a promising technique for retrieval and integration of data from distributed, autonomous and possibly heterogeneous information sources [Squ95]. A warehouse is a repository of integrated information that is available for queries. As relevant information sources are modified, the new information is extracted, and translated to the data model of the warehouse, and integrated with the existing warehouse data. In this paper, we focus on the detection and the extraction of the modifications to the information sources.

The detection and extraction of modifications depends on the facilities at the source. If the source is sophisticated, say a relational database system with triggers, then this process is relatively easy. In many cases, however, the source does not have advanced facilities available for detecting and recording modifications (e.g., legacy sources). If this is the case there are essentially three ways to detect and extract modifications [IC94]:

1. The application running on top of the source is altered to send the modifications to the warehouse.
2. A system log file is parsed to obtain the relevant modifications (as done in the IBM Data Propagator [Gol95]), to the application.
3. The modifications are inferred by comparing a current source snapshot with an earlier one. We call the problem of detecting differences between two source snapshots the snapshot differential problem; it is the problem we address in this paper.

Although the first two methods are usually preferred, both methods have limitations and disadvantages. The first method requires that existing code be altered. In most cases, however, the code is so shopworn that additional modifications are problematic. The second method also has its difficulties. For instance, it is often the case that DBA privileges are required to access the log, so site administrators are reluctant to provide access.

We stress that we are not arguing in favor of snapshot differentials as the best solution for reporting modifications to a warehouse. It clearly does not
scale well: as the volume of source data grows, we have to perform larger and larger comparisons. We are saying, however, that it is a solution we are stuck with for the foreseeable future, and because differentials are such inherently expensive operations it is absolutely critical that we perform them as efficiently as possible. In this paper we will present very efficient differential algorithms; they perform so well because they exploit the particular semantics of the problem.

1.1 Problem Formulation

We view a source snapshot as a file containing a set of distinct records. The file is of the form \( \{R_1, R_2, ..., R_n\} \) where \( R_i \) denote the records. Each \( R_i \) is of the form \(< K, B>\), where \( K \) is the key and \( B \) is the rest of the record representing one or more fields. Without loss of generality, we refer to \( B \) as a single field in the rest of the paper. (In [LGM95] we extend the algorithms presented in this paper to the case where records do not have unique keys.)

For the snapshot differential problem we have two snapshots, \( F_1 \) and \( F_2 \) (the later snapshot). Our goal is to produce a file \( F\text{OUT} \) that also has the form \( \{R_1, R_2, ..., R_n\} \) and each modification record \( R_i \) has one of the following three forms.

1. \(<\text{Update}, K_i, B_j>\)
2. \(<\text{Delete}, K_i>\)
3. \(<\text{Insert}, K_i, B_i>\)

The first form is produced when a record \(<K_i, B_i>\) in file \( F_1 \) is updated to \(<K_i, B_j>\) in file \( F_2 \). The second form is produced when a record \(<K_i, B_i>\) in \( F_1 \) does not appear in \( F_2 \). Lastly, the third form is produced when a record \(<K_i, B_i>\) in \( F_2 \) was not present in \( F_1 \). We refer to the first form as updates, the second as deletes and the third as inserts. The first field is only necessary in distinguishing between updates and inserts. It is included for clarity in the case of deletes.

Conceptually, we have represented snapshots as sets because the physical location of a record within a snapshot file may change from one snapshot to another. That is, records with matching keys are not expected to be in the same physical position in \( F_1 \) and \( F_2 \). This is because the source is free to reorganize its storage between snapshots. Also, insertions and deletions may also change physical record positions in the snapshot.

The snapshot differential can be performed at the source itself. That is, a snapshot is taken periodically and stored at the source site. A daemon process then performs the snapshot differential periodically and sends the detected modifications to the warehouse. The snapshot differential can also be performed at an intermediate site. That is, the source sends the full snapshots to an intermediate site where the snapshot differential process is performed. In any case, the exact procedure for sending these modifications to the data warehouse is implementation dependent.

It is important to realize that there is no unique set of modifications that captures the difference between two snapshots. At one extreme, a deletion can be reported for each record in \( F_1 \) and an insertion can be reported for each record in \( F_2 \). Obviously, this can be wasteful. We capture this notion of wasted messages by defining useless delete-insert pairs and useless insert-delete pairs. A useless insert-delete pair is a message sequence composed of \(<\text{Insert}, K_i, B_i>\) followed (not necessarily immediately) by \(<\text{Delete}, K_i>\), produced when the two snapshots both have a record \(<K_i, B_i>\) or when the earlier snapshot has \(<K_i, B_j>\) and the later one has \(<K_i, B_i>\). A useless insert-delete pair introduces a correctness problem. When the insert is processed at the warehouse, it will most likely be ignored since a record with the same key already exists. Thus, when the delete is processed, the record with the key \( K_i \) will be deleted from the warehouse. On the other hand, a useless delete-insert pair (which is composed of the opposite sequence) does not compromise the correctness of the warehouse. However, it introduces overhead in processing messages since either no modifications were needed (when the two snapshots both have a a record \(<K_i, B_i>\) or the modification could have been reported more succinctly by \(<\text{Update}, K_i, B_i>\).

Since useless pairs are not an effective way of reporting changes, one may be tempted to require snapshot differential algorithms to generate no useless pairs. However, strictly forbidding useless delete-insert pairs turns out to be counterproductive! Allowing the generation of “some” useless delete-insert pairs gives the differential algorithm significant flexibility and leads to solutions that can be very efficient in some cases. We return to these issues later when we quantify the savings of “flexible” differential algorithms over algorithms that do not allow useless delete-insert pairs. Thus, in this paper we do allow useless delete-insert pairs, with the ultimate goal of keeping their numbers relatively small.

However, we do want to avoid useless insert-delete pairs since they may compromise correctness. Useless insert-delete pairs can be eliminated by batching the deletes together and sending the deletes first to the warehouse for processing. In essence, we have transformed the insert-delete pairs into delete-insert
pairs. This method also amortizes the overhead cost of sending the modifications over the network. We assume for the rest of the paper that all useless insert-delete pairs are eliminated.

1.2 Differences with Joins

The snapshot differential problem is closely related to the problem of performing a join between two relations. In particular, if we outerjoin \( F1 \) and \( F2 \) on their common \( K \) attribute on the condition that their \( B \) attributes differ, we can obtain the update records required for the differential problem.

Outerjoin is so closely related to the differential problem that the traditional, ad hoc, join algorithms ([ME92], [HC94]) can be adapted to our needs. Indeed, in Section 3 we show these modifications. However, given the particular semantics and intended application of the differential algorithms, we can go beyond the ad hoc solutions and obtain new and more efficient algorithms. The three main ideas we exploit are as follows:

- Some useless delete-insert pairs are acceptable. Traditional outerjoin algorithms do not have useless delete-insert pairs. The extra flexibility we have allows algorithms that are “ sloppy” but efficient in matching records.

- For some data warehousing applications, it may be acceptable to miss a few of the modifications. Thus, for differentials we can use probabilistic algorithms that may miss some differences (with arbitrarily low probability), but that can be much more efficient. Again, traditional algorithms are not allowed any “ errors,” must be very conservative, and must pay the price.

- Snapshot differentials are an on-going process running at a source. This makes it possible to save some of the information used in one differential to improve the next iteration.

2 Related Work

Snapshots were first introduced in [AL80]. Snapshots were then used in the System \( R^* \) project at IBM Research in San Jose [Loh85]. The data warehouse snapshot can be updated by maintaining a log of the modifications to the database. This approach was defined to be a \textit{differential refresh} strategy in [KR87]. If snapshots were sent periodically, this was called the \textit{full refresh} strategy. In this paper we only consider the case where the source strategy is \textit{full refresh}. [Lee86] also presented a method for refreshing a snapshot that minimizes the number of messages sent when refreshing a snapshot. The method requires annotating the base tables with two columns for a tuple address and a timestamp. We cannot adopt this method in data warehousing since the sources are autonomous.

Reference [CRGMS96] investigates algorithms to find differences in hierarchical structures (e.g., documents, CAD designs). Our focus here is on simpler, record structured differences, and on dealing with very large snapshots that may not fit in memory.

There has been recent complementary work on copy detection of files and documents ([MW94], [BDGM95], [SGM95]). The snapshot differential problem is concerned with detecting the specific differences of two files as opposed to measuring how different two files are. Also related are [BGMF88] and [FWJ86], which propose methods for finding differing pages in files. However, these methods can only detect a few modifications.

The snapshot differential problem is also related to text comparison, for example, as implemented by UNIX \textit{diff} and DOS \textit{comp}. However, the text comparison problem is concerned with a \textit{sequence} of the records, while the snapshot differential problem is concerned with a \textit{set} of records. Reference [HT77] outlines an algorithm that finds the longest common subsequence of the lines of the text, which is used in the UNIX \textit{diff}. Report [LGM95] takes a closer look at how this algorithm can be adopted to solve the snapshot differential problem, although the solution is not as efficient as the ones presented here.

The methods for solving the snapshot differential problem proposed here are based on ad hoc joins which have been well studied; [ME92] and [Sha86] are good surveys on join processing. The snapshot differential algorithms proposed here are used in the data warehousing system \textit{WHIPS}. An overview of the system is presented in [HGWM+95]. After the modifications of multiple sources are detected, the modifications are integrated using methods discussed in [ZGMHW95].

Note that there are also cases wherein knowledge of the semantics of the information maintained at the warehouse helps make change detection simpler. An outline of these special cases is in report [LGM95).

3 Using Compression

In this section we first describe existing, ad hoc, join algorithms but we do not cover all the known variations and optimizations of these algorithms. We believe that many of these further optimizations can also be applied to the snapshot differential algo-
After extending the ad hoc algorithms to handle the differential problem, we study record compression techniques to optimize them. In the sections below, we denote the size of a file \( F \) as \(|F|\) blocks and the size of main memory as \(|M|\) blocks. We also exclude the cost of writing the output file in our cost analysis since it is the same for all of the algorithms.

### 3.1 Outer Join Algorithms

The basic sort merge join first sorts the two input files. It then scans the files once and any pair of records that satisfy the join condition are produced as output. The algorithm can be adapted to perform an outer join by identifying the records that do not join with any records in the other file during the scan. This can be done with no extra cost when two records are being matched: the record with the smaller key is guaranteed to have no matching records.

Since differentials are an on-going process running at a source, it is possible to save the sorted file of the previous snapshot. Thus, the algorithm only needs to sort the second file, \( F_2 \). This can be done using the multiway merge-sort algorithm. This algorithm constructs runs which are sequences of blocks with sorted records. After a series of passes, the file is partitioned into progressively longer runs. The algorithm terminates when there is only one run left. In general, it takes \( 2 \times |F| \times \log_M |F| \) IO operations to sort a file with size \(|F|\) ([Ul89]). However, if there is enough main memory \((|M| > \sqrt{|F|})\), the sorting can be done in \( 4 \times |F| \) IO operations (sorting is done in two passes). The second phase of the algorithm, which involves scanning and merging the two sorted files, entails \(|F_1| + |F_2| \) IO operations for a total of \(|F_1| + 5 \times |F_2|\) IO operations.

The \( IO \) cost can be reduced further by just producing the sorted runs (denoted as \( F_{2 \_runs} \)) in the first phase. The first step of the algorithm produces the sorted \( F_2 \) runs, at a cost of only \( 2 \times |F_2| \) IOs. \((\text{File } F_1 \text{ has already been sorted at this point.})\). The sorted \( F_2 \) file, needed for the next run of the algorithm, can then be produced while matching \( F_{2 \_runs} \) with \( F_1 \). In producing the sorted \( F_2 \) file, we read into memory one block from each run in \( F_{2 \_runs} \) (if the block is not already in memory), and select the record with the smallest \( K \) value. The merge process then costs \( 2 \times |F_2| + |F_1| \) IOs. The total cost incurred is \(|F_1| + 4 \times |F_2|\) IOs.

Another method that we discuss here is the partitioned hash join algorithm. In the partitioned hash join algorithm, the input files are partitioned into buckets by computing a hash function on the join attribute. Records are matched by considering each pair of corresponding buckets. First, one of the buckets is read into memory (the smaller one) and an in-memory hash table is built (assuming the bucket fits in memory). The second bucket is then read and a probe into the in-memory hash table is made for each record in an attempt to find a matching record in the first bucket. A more detailed discussion of the partitioned hash algorithm is found in [LGM96] where we also show that the \( IO \) cost incurred is \(|F_1| + 3 \times |F_2|\).

### 3.2 Compression Techniques

Our compression algorithms reduce the sizes of records and the required \( IO \). Compression can be performed in varying degrees. For instance, compression may be performed on the records of a file by compressing the whole record (possibly excluding the key field) into \( n \) bits. A block or a group of blocks can be compressed into \( n \) bits. There are also numerous ways to perform compression such as computing the check sum of the data and hashing the data to obtain an integer. Compression can also be lossy or lossless. In the latter case, the compression function guarantees that two different uncompressed values are mapped into different compressed values. Lossy compression functions do not have this guarantee but have the potential of achieving higher compression factors. Henceforth, we assume that we are using a lossy compression function. We ignore the details of the compression function and simply refer to it as \( \text{compress}(x) \).

There are a number of benefits from processing compressed data. First of all, the compressed intermediate files, such as the buckets for the partitioned hash join, are smaller. Thus, there will be fewer \( IO \) when reading the intermediate files. Moreover, the compressed file may be small enough to fit in memory. Even if the compressed file does not fit entirely in memory, some of the join algorithms may still benefit. For example, the compressed file may result in buckets that fit in memory which improves the matching phase of the partitioned hash join algorithm.

Compression is not without its disadvantages. As mentioned earlier, a lossy compression function may map two different records into the same compressed value. This means that the snapshot differential algorithm is probabilistic and may not be able to detect all the modifications to a snapshot. We now show that this can occur with a probability of \( 2^{-n} \), where \( n \) is the number of bits for the compressed value. Assume that we are compressing an object (which may be the \( B \) field, or the entire record, or...
an entire block, etc.) of $b$ bits ($b > n$). There are then $2^b$ possible values for this object. Since there are only $2^n$ values that the compressed object can attain, there are $2^b/2^n$ original values mapped to each compressed value. Thus for each given original value, the probability that another value maps to the same compressed value is $((2^b/2^n) - 1)/2^n$, which is approximately $2^{-n}$ for large values of $b$. For sufficiently large values of $n$, this probability can be made very small. The expression $2^{-n}$, henceforth denoted as $E$, gives the probability that a single comparison is erroneous. For example, if the $B$ field of the record $<K, B>$ is compressed into a 32-bit integer, the probability that a single comparison (of two $B$ fields) is erroneous is $2^{-32}$ or approximately $2.3 \times 10^{-10}$. However, as we compare more records, the likelihood that a modification is missed increases. To put this probability of error into perspective, let us suppose we perform a differential on two 256 MB snapshots daily. We now proceed to compute how many days we expect to pass before a record modification is missed. We first compute the probability (denoted as $p_{day}$) that there is no error in comparing two given snapshots. Let us suppose that the record size is 150 bytes which means that there are approximately 1,789,570 records for each file.

$$p_{day} = (1 - E)^{records(F)} = (1 - 2.3 \times 10^{-10})^{1,789,570}$$

Using this probability, we can compute the expected number of days before an error occurs.

$$N_{good\ days} = (1 - p_{day}) \times \sum_{i=0}^{j} i \times p_{day}^{i-1} = \frac{1}{1 - p_{day}}$$

This comes out to be 2,430 days, or more than 6.7 years! We believe that for some types of warehousing applications, such as data mining, this error rate will be acceptable.

It is evident from the equations above that as the number of records increases, the expected number of days before an error occurs goes down. However, as the number of bits used for compressing the $B$ field is increased, the expected number of years before an error occurs can be made comfortably large even for large files.

For the algorithms we will present here, we consider two ways of compressing the records. For both compression formats, we do not compress the key, and we denote the compressed $B$ field as $b$. The first format is simply compress a record $<K, B>$ into $<K, b>$. For the second format, the only difference is that a pointer is appended forming the record $<K, b, p>$. The pointer $p$ points to the correspond-

**Algorithm 3.1**

**Input** $F_1\ sorted$, $F_2$

**Output** $F_{out}$ (the snapshot differential), $F_2\ sorted$

**Method**

1. $F_2\ runs \leftarrow SortIntoRuns(F_2)$
2. $r_1 \leftarrow$ read the next record from $F_1\ sorted$
3. $r_2 \leftarrow$ read the next record from $F_2\ runs$
4. $F_{sorted} \leftarrow Output(<Insert, r_2, K, r_2, B>)$
5. $r_2 \leftarrow$ read the next record from $F_2\ runs$:
6. $F_{sorted} \leftarrow Output(<Insert, r_2, K, r_2, B>)$
7. $F_{sorted} \leftarrow Output(<Insert, r_2, K, r_2, B>)$
8. else if $((r_2 = NULL) \lor (r_2 < K, K))$ then
9. $F_{sorted} \leftarrow Output(<Delete, r_1, K>)$
10. $r_1 \leftarrow$ read the next record from $F_1\ sorted$
11. else if $((r_2 = K, K))$ then
12. $F_{sorted} \leftarrow Output(<Update, r_2, K, r_2, B>)$
13. $r_1 \leftarrow$ read the next record from $F_1\ sorted$
14. $r_2 \leftarrow$ read the next record from $F_2\ sorted$
15. $F_{sorted} \leftarrow Output(<Insert, r_2, K, r_2, B>)$

Figure 1: Sort Merge Outerjoin Enhanced with the $<K, b>$ Compression Format

We now augment the sort merge outerjoin with compression (shown in Figure 1). The algorithm differs from the standard sort-merge algorithm in that it reads a compressed sorted $F_1$ file (denoted as $F_1\ sorted$, with a size of $|F_1|/u$). Also, when detecting the updates in step (12), the compressed versions of the $B$ field are compared. Lastly, steps (3), (7) and (15) now first compress the $B$ field before producing an output into $F_2\ sorted$.

The sorting phase of the algorithm incurs $2 \cdot |F_2| I/Os$ The matching phase (steps (4) onwards) incurs $|F_2| + |F_1| I/Os$ since the two files are scanned once. Lastly, the sorted $F_2\ sorted$ must be produced for the next differential, which costs $|F_2| I/Os$. The total cost is then $|F_1| + 3 \cdot |F_2| + |F_2| I/Os$.

Greatest improvements may be achieved by compressing not only the first snapshot but also the second snapshot before the files are matched. When the second snapshot arrives, it is read into memory and compressed sorted runs are written out.
Algorithm 3.2
Input $f_1$ sorted, $F_2$
Output $F_{out}$ (the snapshot differential), $F_2$ sorted
Method
1. $f_2_{runs} \leftarrow \text{SortIntoRuns}\,\text{Compress}(F_2)$
2. $r_2 \leftarrow$ read the next record from $f_1$ sorted
3. $r_2 \leftarrow$ read the next record from $f_2_{runs}$
   $F_{sorted} \leftarrow \text{Output}(<r_2, K, r_2.b, r_2.p>)$
4. while $((r_1 \neq NULL) \land (r_2 \neq NULL))$
5. if $((r_1 = NULL) \lor (r_1.K > r_2.K))$
   5a. $r_{full} \leftarrow$ read tuple in $F_2$ with address $r_2.p$
   6. $F_{out} \leftarrow \text{Output}(<\text{Insert}, r_2.K, r_{full.B}>)$
   7. $r_2 \leftarrow$ read the next record from $f_2_{runs}$
   $F_{sorted} \leftarrow \text{Output}(<r_2, K, r_2.b, r_2.p>)$
8. else if $((r_2 = NULL) \lor (r_1.K < r_2.K))$
   9. $F_{out} \leftarrow \text{Output}(<\text{Delete}, r_1.K>)$
10. $r_1 \leftarrow$ read the next record from $f_1$ sorted
11. else if $(r_1.K = r_2.K)$
12. if $(r_1.b \neq r_2.b)$
   12a. $r_{full} \leftarrow$ read tuple in $F_2$ with address $r_2.p$
   13. $F_{out} \leftarrow \text{Output}(<\text{Update}, r_2.K, r_{full.B}>)$
   14. $r_1 \leftarrow$ read the next record from $f_1$ sorted
   15. $r_2 \leftarrow$ read the next record from $f_2_{runs}$
   $F_{sorted} \leftarrow \text{Output}(<r_2, K, r_2.b, r_2.p>)$
\hfill \Box

Figure 2: Sort Merge Outerjoin Enhanced with the $<K, b, p>$ Compression Format

essence, the uncompressed $F_2$ file is read only once.
The problem introduced by compressing the second snapshot is that when insertions and updates are detected, the original uncompressed record must be obtained from $F_2$. In order to find the original (uncompressed) record, a pointer to the record must be saved in the compressed record. Thus, for this algorithm, the $<K, b, p>$ compression format must be used. The full algorithm is shown in Figure 2. Step (5a) (step(12a)) shows that when an insertion (update) is detected, the pointer $p$ of the current record is used to obtain the original record in order to produce the correct output.

Step (1) of Algorithm 3.2 only incurs $|F_2| + |f_2| \text{ IOs}$ instead of $2 \times |F_2| \text{ IOs}$. Steps (4) through (15) incur $|f_1| + |f_2| + U + I \text{ IOs}$, where $U$ and $I$ are the number of updates and insertions found. An additional $|F_2| \text{ IOs}$ are needed to write out the sorted $f_2$ file. As a result, the overall cost is $|f_1| + |F_2| + 3 \times |f_2| + U + I$. The savings in IO cost is significant especially if there are few updates and inserts.

The partitioned hash outerjoin is augmented with compression in a very similar manner to the sort merge outerjoin. We show in [LGM96] that the overall cost is reduced to $|f_1| + 3 \times |F_2| + |f_2| \text{ IOs}$ if the buckets are compressed after the matching phase. If the buckets are compressed before the matching phase, we also show in [LGM96] that the overall cost is $|f_1| + |F_2| + 2 \times |f_2| + U + I \text{ IOs}$.

The performance gains can even be greater if the compression factor $n$ is high enough such that all of the buckets of $F_1$ fit in memory. In this case, all the buckets for $F_1$ are simply read into memory ($|f_1| \text{ IOs}$). The file $F_2$ is then scanned, and for each record in $F_2$ read, the in-memory buckets are probed. The compressed buckets for $F_2$ can also be constructed for the next differential during this probe. The overall cost of this algorithm is only $|f_1| + |F_2| + |f_2| \text{ IOs}$.

4 The Window Algorithm

In the previous section, we described algorithms that compute the differential of two snapshots based on ad hoc join algorithms. We saw that the snapshots are read multiple times. Since the files are large, reading the snapshots multiple times can be costly. We now present an algorithm that reads the snap-
shots exactly once. This new algorithm assumes that matching records are physically “nearby” in the files. As mentioned in Section 1, matching records cannot be expected to be in the same position in the two snapshots, due to possible reorganizations at the source. However, we may still expect a record to remain in a relatively small area, such as a block, cylinder, or track. This is because file reorganization algorithms typically rearrange records within a physical sub-unit. The window algorithm takes advantage of this, and of ever increasing main memory capacity, by maintaining a moving window of records in memory for each snapshot. Only the records within the window are compared in the hope that the matching records occur within the window. Unmatched records are reported as either an insert or a delete, which can lead to useless delete-insert pairs. As discussed in Section 1, a small number of these may be tolerable.

For the window algorithm, we divide available memory into four distinct parts as shown in Figure 3. Each snapshot has its own input buffer (input buffer 1 is for $F_1$) and aging buffer. The input buffer is simply the buffer used in transferring blocks from disk. The aging buffer is essentially the moving window mentioned above.

The algorithm is shown in Figure 4 and we now proceed to explain each step. Steps (1) and (2) simply reads a constant number of input block of records from file $F_1$ and file $F_2$ to fill input buffer 1 and input buffer 2, respectively. This process will be done repeatedly by steps (9) and (10). Before the input buffers are refilled, the algorithm guarantees that they are empty. Steps (4) through (6) are concerned with matching the records of the two snapshots. In Step (4), the matching is performed in a nested loop fashion. This is not expensive since the input buffers are relatively small. The matched records can produce updates if the $B$ fields differ. The slots that these matching records occupy in the buffer are also marked as free. In step (5), the remaining records in input buffer 1 are matched against aging buffer 2. Since the aging buffers are much larger, the aging buffers are actually hash tables to make the matching more efficient. For each remaining record in input buffer 1, the hash table that is aging buffer 2 is probed for a match. As in step (4), an update may be produced by this matching. The slots of the matching records are also marked as free. Step (6) is analogous to step (5) but this time matching input buffer 2 and aging buffer 1. Steps (7) and (8) clear both input buffers by forcing the unmatched records in the input buffers into their respective aging buffers. The same hash function used in steps (4) and (5) is used to determine which bucket the record is placed into. Since new records are forced into the aging buffer, some of the old records in the aging buffer may be displaced. These displaced records constitute the deletes (inserts) if the records are displaced from input buffer 1 (input buffer 2). The displacement of old records is explained further below. The steps are then repeated until both snapshots are processed. At that point, any remaining records in the aging buffers are output as inserts or deletes.

In the hash table that constitutes the aging buffer there is an embedded “aging” queue, with the head of the queue being the oldest record in the buffer, and the tail being the youngest. Figure 3 illustrates the aging buffer. Each entry in the hash table has a timestamp associated with it for illustration purposes only. The figure shows that the oldest record (with the smallest timestamp) is at the head of the queue. Whenever new records are forced into the aging buffer, the new records are placed at the tail of the queue. If the aging buffer is full, the record at the head of the queue is displaced as a new record is enqueued at the tail. This action produces a delete (insert) if the buffer in question is aging buffer 1 (aging buffer 2).

Since files are read once, the IO cost for the window algorithm is only $|F_1| + |F_2|$ regardless of memory size, snapshot size and number of updates and inserts. Thus the window algorithm achieves the optimal IO performance if compression is not considered. However, the window algorithm can produce useless delete-insert pairs in Steps 6 and 7 of the algorithm. Intuitively, the number of useless delete-insert pairs produced depends on how physically different the two snapshots are.

To quantify this difference, we define the concept of the distance of two snapshots. We want the distance measure to be symmetric and independent of the size of the file. The equation below exhibits the two desired properties.

$$distance = \frac{\sum_{R_1 \in F_1, R_2 \in F_2, match(R_1, R_2)} |pos(R_1) - pos(R_2)|}{\max(\text{records}(F_1), \text{records}(F_2))^{2/2}}$$

The function pos returns the physical position of a record in a snapshot. The boolean function match is true when records $R_1$ and $R_2$ have matching keys. The function records returns the number of records of a snapshot file. Thus, this equation sums up the absolute value of the difference in position of the matching records and normalizes it by the maximum distance for the given snapshot file sizes. The maximum distance between two snapshots is attained when the records in the second snapshot are in the opposite order (the first record is exchanged with
the last record, the second record with the second to the last, and so on) relative to the first snapshot. If \( \text{records}(F_1) = \text{records}(F_2) \), it is easy to see that in the worst case the average displacement of each record is \( \text{records}(F_1)/2 \), and hence the maximum distance is \( \text{records}(F_1)^2/2 \). If the files are of different sizes, using the larger of the two files gives an upper bound on the maximum distance. Our distance metric will be used in the following section to evaluate the window algorithm.

5 Performance Evaluation

5.1 Analytical IO Comparison

We have outlined in the previous section algorithms that can compute a snapshot differential: performing sort merge outerjoin (SM), performing a partitioned hash outerjoin (PH), performing a sort merge outerjoin with two kinds of record compression (SMC1, SMC2), performing partitioned hash outerjoin with two kinds of record compression (PHC1, PHC2) and using the window algorithm (W). SMC1 denotes sort merge outerjoin with a record compression format of \(<K, b>\) (similarly for PHC1); SMC2 uses the record compression format \(<K, b, p>\) (similarly for PHC2). In this section, we will illustrate and compare the algorithms in terms of IO cost, size of intermediate files, and the probability of error. Due to space limitations, this is not a comprehensive study, but simply an illustration of potential differences between the algorithms in a few realistic scenarios.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Default</th>
</tr>
</thead>
<tbody>
<tr>
<td>( M )</td>
<td>Memory Size</td>
<td>32 MB</td>
</tr>
<tr>
<td>( B )</td>
<td>Block Size</td>
<td>16K</td>
</tr>
<tr>
<td>( F )</td>
<td>File Size</td>
<td>256 MB or 1024 MB</td>
</tr>
<tr>
<td>( R )</td>
<td>Record Size</td>
<td>150 bytes</td>
</tr>
<tr>
<td>( \text{records}(F) )</td>
<td>Number of Records</td>
<td>1,780,569 or 7,158,279</td>
</tr>
<tr>
<td>( r )</td>
<td>Compressed Record Size</td>
<td>10 or 14 bytes</td>
</tr>
<tr>
<td>( u )</td>
<td>Compression Factor</td>
<td>15 or 10</td>
</tr>
<tr>
<td>( \text{U}+\text{I} )</td>
<td>Number of Inserts and Updates</td>
<td>1% of ( \text{records}(F) )</td>
</tr>
<tr>
<td>( IO )</td>
<td>Number of IOs</td>
<td>N/A</td>
</tr>
<tr>
<td>( X )</td>
<td>Intermediate File Size</td>
<td>N/A</td>
</tr>
<tr>
<td>( E )</td>
<td>Probability of Error</td>
<td>N/A</td>
</tr>
</tbody>
</table>

Figure 5 shows the variables that will be used in comparing the algorithms. We assume that the snapshots have the same number of records. The number of records (\( \text{records}(F) \)) are calculated using \( F/R \), where \( R \) is the record size (150 bytes). The compressed record size is 10 bytes for the \(<K, b>\) format and 14 bytes for the \(<K, b, p>\) format. This leads to compression factors of 15 and 10 respectively.

Figure 6 shows a summary of the results computed for the various algorithms. The two columns labeled \( IO_{256} \) and \( IO_{1024} \) show the IO cost incurred in processing 256 MB and 1024 MB snapshots for the different algorithms. Using the sort merge outerjoin as a baseline, we can see that the partitioned hash outerjoin (PH) reduces the IO cost by 20%. Compression using the \(<K, b>\) record format achieves a 37% reduction in IO cost over sort merge using SMC1, and a 50% reduction using SMC2. For the 256 MB file, the compressed file fits in memory which enables the PHC1 and PHC2 algorithms to build a complete in-memory hash table, as explained in Section 3.3. The reduction in IO cost for these two algorithms, in this case, surpasses even that of the window algorithm.

However, when the larger file is considered, the compressed file no longer fits in the 32 MB memory. Thus the PHC1 and PHC2 algorithms achieve more modest reductions in this case (37% and 52% respectively). Other than these two algorithms, the reductions achieved by the other algorithms are unchanged even with the larger file.

Figure 7 shows how the algorithms compare when the size of the snapshots is varied over a range. The values of other parameters are unchanged. Note that we have not plotted SMC1 and SMC2 since their plots are almost indistinguishable from PHC1 and
$PHC2$ respectively beyond a file size of 500 MB. Also note the discontinuity in the graph for $PHC1$ and $PHC2$. $PHC1$ is able to build an in-memory hash table if the file is smaller than 500 MB (and files smaller than 320 MB for $PHC2$). If the partitioned hash join algorithms are able to build an in-memory hash table, they can even outperform the window algorithm.

Clearly, the IO savings for compression algorithms depend on the compression factor. Figure 8 illustrates that when the compression factor is low, the algorithms with compression perform worse than $PH$ (even worse than $SM$ in case of $SMC1$ and $SMC2$). The other point that this graph illustrates is that the benefits of compression are bounded. Thus, going beyond a factor of 10 in this case does not buy us much.

The performance of the compression algorithms that use the pointer format (algorithms $PHC2$ and $SMC2$) depend on the number of updates and inserts. If $U + I$ is higher than what we have assumed, $PHC1$ and $SMC1$ outperform $PHC2$ and $SMC2$. Figure 9 shows the performance of the algorithms with different $U + I$. This shows that $PHC2$ and $SMC2$ are only useful for scenarios with relatively few modifications between snapshots (less than say 2 percent of the records). By manipulating the IO cost equations, it is not hard to show that if $U + I$ is greater than 1.7%, $PHC1$ and $SMC1$ incur less IO than $PHC2$ and $SMC2$.

The next two columns in Figure 6 ($X_{10}$ and $X_{25}$) examine the size of the intermediate files. In the case of the $SM$, $PH$, $SMC1$ and $PHC1$ algorithms, uncompressed intermediate files need to be saved. In the case of the $SMC2$ and $PHC2$ algorithms, the compressed versions of these files are constructed, which leads to a more economic disk usage. The window algorithm, on the other hand, does not construct any intermediate files.

The last column (labeled $E$) illustrates the probability of a missed matching record pair. Note that both record compression formats result in the same probability of error although the two formats have different compression factors. This is because the $B$ field is compressed into a 32 bit integer for both formats.

In closing this section, we stress that the num-

---

**Figure 6: Comparison of Algorithms**

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>$IO_{256}$ (% savings)</th>
<th>$IO_{1024}$ (% savings)</th>
<th>$X_{256}$ (MB)</th>
<th>$X_{1024}$ (MB)</th>
<th>Probability of Error ($E$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$SM$</td>
<td>81,920</td>
<td>327,680</td>
<td>16384</td>
<td>65,536</td>
<td>0</td>
</tr>
<tr>
<td>$SMC1$</td>
<td>51,336 (37%)</td>
<td>205,346 (37%)</td>
<td>16,384</td>
<td>65,536</td>
<td>$2.3 \times 10^{-10}$</td>
</tr>
<tr>
<td>$SMC2$</td>
<td>40,883 (50%)</td>
<td>163,333 (50%)</td>
<td>1,639</td>
<td>6,554</td>
<td>$2.3 \times 10^{-10}$</td>
</tr>
<tr>
<td>$PH$</td>
<td>65,536 (20%)</td>
<td>262,144 (20%)</td>
<td>16,384</td>
<td>65,536</td>
<td>0</td>
</tr>
<tr>
<td>$PHC1$</td>
<td>18,568 (77%)</td>
<td>205,346 (31%)</td>
<td>16,384</td>
<td>65,536</td>
<td>$2.3 \times 10^{-10}$</td>
</tr>
<tr>
<td>$PHC2$</td>
<td>19,660 (76%)</td>
<td>156,779 (52%)</td>
<td>1,639</td>
<td>6,554</td>
<td>$2.3 \times 10^{-10}$</td>
</tr>
</tbody>
</table>

---

**Figure 8: IO Cost and Compression Factor**

**Figure 9: IO Cost and Varying Update and Insertion Rates**

$SMC2$ are only useful for scenarios with relatively few modifications between snapshots (less than say 2 percent of the records). By manipulating the IO cost equations, it is not hard to show that if $U + I$ is greater than 1.7%, $PHC1$ and $SMC1$ incur less IO than $PHC2$ and $SMC2$.

The window algorithm, on the other hand, does not construct any intermediate files.

The last column (labeled $E$) illustrates the probability of a missed matching record pair. Note that both record compression formats result in the same probability of error although the two formats have different compression factors. This is because the $B$ field is compressed into a 32 bit integer for both formats.
<table>
<thead>
<tr>
<th>Window Parameters</th>
<th>Default Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>$AB$ Aging Buffer Size</td>
<td>8 MB</td>
</tr>
<tr>
<td>$IB$ Input Block Size</td>
<td>16K</td>
</tr>
</tbody>
</table>

Figure 10: List of Parameters

numbers we have shown are only illustrative. The gains of the various algorithms can vary widely. For example, if we assume very large records, then even modest compression can yield huge improvements. On the other hand, if we assume very large memories (relative to the file sizes), then the gains become negligible.

5.2 Evaluation of Implemented Algorithms

In WHIPS, we have implemented the sort merge outerjoin and the window algorithm to compute the snapshot differentials. We have also built a snapshot differential algorithm evaluation system, which we used to study the effects of the snapshot pair distance on the number of useless delete-insert pairs that is produced by the window algorithm. We will also use the evaluation system to compare the actual running times of the window algorithm and the sort merge outerjoin algorithm.

The evaluation system has a snapshot generator that produces a pair of synthetic snapshots with records of the form $< K, B >$. The snapshot generator produces the two snapshots based on the following parameters: size of the $B$ field, number of records, average record displacement ($disp_{avg}$) and percentage of updates. The first snapshot is constructed to have ordered $K$ fields with the specified number of records and with the specified $B$ field size. Figure 10 shows the default snapshot pair parameters.

Conceptually, the second snapshot is produced by first copying the first snapshot. Each record $R_j$ in the second snapshot is then swapped with a record that is, on average (uniformly distributed from 0 to $2 \times disp_{avg}$), $disp_{avg}$ records away from $R_j$. Based on the specified percentage of updates, some of the records in the second snapshot are modified to simulate updates. Insertions and deletions are not generated since they do not affect the number of useless delete-insert pairs produced. Notice that $disp_{avg}$ is not the distance measure between snapshots. It is a generator parameter that indirectly affects the resulting distance. Thus, after generating the two snapshots, the actual distance of the two snapshots is then measured.

The two snapshots along with algorithm specific parameters are passed to the snapshot differential algorithm being tested. Note that any of the previous algorithms discussed can be used as the snapshot differential algorithm. In the experiments that we present here we focus on the window and the sort merge outerjoin algorithms. By varying the aging buffer size and the input buffer size parameters, we can study how these parameters affect the window algorithm. Figure 10 also shows the default window parameters. These were used unless the parameter was varied in an experiment.

After the snapshot differential algorithm is run, the output of the algorithm is compared to what was "produced" by the snapshot generator. Since the snapshot generator synthesized the two snapshots, it also knows the minimal set of differences of the two snapshots. The message comparator can then check for the correctness of the output and count the number of extra messages.

The experiments we conducted enable us to evaluate, given the size of the aging buffer, and the size and the distance of the snapshots, how well the window algorithm will perform in terms of the number of extra messages produced. In the first experiment, we varied the $disp_{avg}$ (and indirectly the distance) and measured the number of extra messages produced. This experiment was performed on three pairs of snapshots whose sizes ranged from 50 MB to 100 MB. Figure 11 shows that, as expected, as the distance of the snapshots increases beyond the capacity of the aging buffer, the number of extra
messages increases. As the number of extra messages sharply rises, the graphs exhibit strong fluctuations. This is because the synthetic snapshots were produced randomly and only one experiment was done for each distance. For each snapshot size, there is a critical distance \( \text{dist}_{\text{crit}} \) which causes the \textit{window} algorithm to start producing extra messages with the given aging buffer size.

For a system designer, it is helpful to translate \( \text{dist}_{\text{crit}} \) into a critical average physical displacement. For instance, if the designer knows that records can only be displaced within a cylinder and the designer can only allocate 8 MB to each aging buffer, it is useful to know if the \textit{window} algorithm produces few useless delete-insert messages in this scenario. We now capture this notion by first manipulating the definition of distance (equation (3) in Section 4) to show that \( \text{dist}_{\text{crit}} \) of the different snapshot pairs can be translated into a critical average physical displacement (in terms of MB). Since there are no insertions or deletions in the synthetic snapshot pair, we can define a critical average record displacement (denoted as \( \text{disp}_{\text{crit}} \)) which is related to \( \text{dist}_{\text{crit}} \) as shown in equation (5).

\[
\text{dist}_{\text{crit}} = \frac{\sum \text{r}_1 \times \text{r}_2 \times \text{match} \left( \text{r}_1, \text{r}_2, \text{pos}(\text{r}_1) - \text{pos}(\text{r}_2) \right)}{\text{records}(F) / 2} = \frac{\text{records}(F) \times \text{disp}_{\text{crit}}}{\text{records}(F) \times \text{records}(F) / 2}
\]

\[
\text{disp}_{\text{crit}}_{\text{MB}} = \text{disp}_{\text{crit}} \times R = \text{dist}_{\text{crit}} \times (\text{records}(F) / 2) \times R
\]

Using the size of the record, we can translate the \( \text{dist}_{\text{crit}} \) into a critical average physical displacement (denoted as \( \text{disp}_{\text{crit}}_{\text{MB}} \) which is in terms of MB) using equation (6). Figure 12 shows the result of the calculations for the different snapshot pairs. The \( \text{dist}_{\text{crit}} \) of the snapshot pairs are estimated from Figure 11. This table shows, for example, that the \textit{window} algorithm can tolerate an average physical displacement of about 11.2 MB given an aging buffer size of only 8 MB to compare 100 MB snapshots. Thus, if a system designer knows that the records can only be displaced within, say a page (which is normally smaller than 11.2 MB), then the designer can be assured that the \textit{window} algorithm will not produce excessive amounts of extra messages.

In the next experiment, we focus on the 100 MB snapshots. Using the parameters listed in Figure 10, we varied the size of the aging buffer from 1.0 MB to 16 MB. The \( \text{disp}_{\text{avg}} \) was set at 50,000 with a resulting distance of 0.34, which is well above the \( \text{dist}_{\text{crit}} \). Figure 13 shows that once the size of the aging buffer is at least 12.8 MB, no extra messages are produced. This is to be expected since we showed previously (Figure 12) that the tolerable \( \text{disp}_{\text{crit}}_{\text{MB}} \) for the 100 MB file is 11.2 MB. Using the same snapshot pair, we also varied the input block size from 8 K to 80 K. The variation had no effect on the number of extra messages and we do not show the graph here. Again, this is to be expected, since the size of the aging buffer is much larger than the size of the input block. Thus, even if the input block size is varied, the window size stays the same. We also varied the record size and this showed no effect on the number of extra messages produced.

\begin{table}[h]
\begin{tabular}{|c|c|c|c|}
\hline
\textbf{File Size} & \textbf{records}(F) & \textbf{dist}_{\text{crit}} & \textbf{disp}_{\text{crit}}_{\text{MB}} \\
\hline
50 MB & 162,500 & 0.44 & 5.11 \\
75 MB & 325,000 & 0.34 & 7.91 \\
100 MB & 650,000 & 0.24 & 11.2 \\
\hline
\end{tabular}
\end{table}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure12.png}
\caption{\textit{dist}_{\text{crit}} and \textit{disp}_{\text{crit}}_{\text{MB}}}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure13.png}
\caption{Effect of the Memory Size on the Number of Extra Messages}
\end{figure}
algorithm is also significantly less CPU intensive than the sort merge based algorithm (e.g., 80s compared to 250s for a 75 MB file). As expected then, Figure 14 shows that the window algorithm outperforms the sort merge outerjoin in terms of clock time. Moreover, Figure 14 also shows that the CPU time is a small fraction of the clock time in the window algorithm. Thus, the IO comparisons of Section 5.1 are indeed useful.

6 Conclusion

We have defined the snapshot differential problem and discussed its importance in data warehousing. All of our proposed algorithms are relatively simple, but we view this as essential for dealing efficiently with large files. In summary, we have the following results:

- By augmenting the outerjoin algorithms with record compression, we have shown that very significant savings in IO cost can be attained.

- We have introduced the window algorithm which works extremely well if the snapshots are not too different. Under this scenario, this algorithm outperforms the join based algorithms and its running time is comparable to simply reading the snapshots once.

We have incorporated the window and the sort merge outerjoin algorithms into the initial WHIPS prototype. The production version of the algorithm takes as input a "format definition" that describes the record format of the snapshots and identifies the key field[s]. The format allows for complex value fields, but the window algorithm will consider the entire record as a single field. We also plan to implement a post-processor that filters out useless delete-insert pairs before they are sent to the warehouse.

The differential algorithm and the warehouse itself are implemented within the Corba distributed object framework, using ILU, an implementation from Xerox PARC [CJS94]. For our system demonstrations, we use the window algorithm to extract modifications from a legacy source that handles financial account information at Stanford. In the future, we will use the algorithm to compare file dumps of company information obtained from various Dialog databases ([Ser94]).

References


